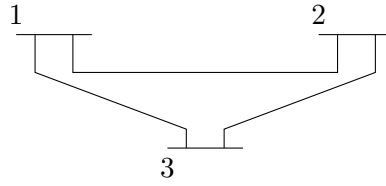


Problem Set - 3
Bus Admittance and Impedance Matrices

1. Form \mathbf{Y}_{Bus} matrix for the network shown here.



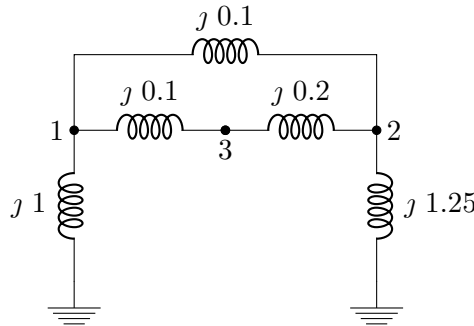
| Line | Series Reactance p.u. | Shunt Admittance p.u. |
|------|-----------------------|-----------------------|
| 1-2 | $j 0.20$ | $j 0.24$ |
| 2-3 | $j 0.10$ | $j 0.16$ |
| 1-3 | $j 0.25$ | $j 0.30$ |

Ans: $\mathbf{Y}_{\text{Bus}} = \begin{pmatrix} -j8.73 & j5 & j4 \\ j5 & -j14.8 & j10 \\ j4 & j10 & -j13.77 \end{pmatrix}$

2. Modify \mathbf{Y}_{BUS} if the line between 1 and 2 is removed.

Ans: $\mathbf{Y}_{\text{Bus}} = \begin{pmatrix} -j3.85 & 0 & j4 \\ 0 & -j9.92 & j10 \\ j4 & j10 & -j13.77 \end{pmatrix}$

3. Form \mathbf{Z}_{BUS} matrix for the network shown here by building algorithm.



Ans: $\mathbf{Z}_{\text{Bus}} = \begin{pmatrix} j0.5699 & j0.5376 & j0.5591 \\ j0.5376 & j0.5780 & j0.5511 \\ j0.5591 & j0.5511 & j0.6231 \end{pmatrix}$

4. Modify \mathbf{Z}_{BUS} if the line between 1 and 2 is removed.

Ans: $\mathbf{Z}_{\text{Bus}} = \begin{pmatrix} j0.6081 & j0.4898 & j0.5686 \\ j0.4898 & j0.6378 & j0.5393 \\ j0.5686 & j0.5393 & j0.6254 \end{pmatrix}$

5. Find the \mathbf{L} and \mathbf{U} triangular factors of the symmetric matrix

$$\mathbf{A} = \begin{pmatrix} 2 & 1 & 3 \\ 1 & 5 & 4 \\ 3 & 4 & 7 \end{pmatrix}$$

Ans: $\mathbf{L} = \begin{pmatrix} 1 & 0 & 0 \\ \frac{1}{2} & 1 & 0 \\ \frac{3}{2} & \frac{5}{9} & 1 \end{pmatrix} \quad \mathbf{U} = \begin{pmatrix} 2 & 1 & 3 \\ 0 & \frac{9}{2} & \frac{5}{2} \\ 0 & 0 & \frac{10}{9} \end{pmatrix}$