CS5201: Advanced Artificial Intelligence

Prolog programming



Arijit Mondal

Dept of Computer Science and Engineering Indian Institute of Technology Patna www.iitp.ac.in/~arijit/

What is Prolog?

- Invented early seventies by Alain Colmerauer in France and Robert Kowalski in Britain
- Prolog = Programmation en Logique (Programming in Logic).
- Prolog is a declarative programming language unlike most common programming languages.
- In a declarative language
 - The programmer specifies a goal to be achieved
 - The Prolog system works out how to achieve it
- In purely declarative languages, the programmer only states what the problem is and leaves the rest to the language system

Relations

- Prolog programs specify relationships among objects and properties of objects
- When we say, "Ayesha owns the pen", we are declaring the ownership relationship between two objects: Ayesha and the pen.
- When we ask, "Does Ayesha own the pen?" we are trying to find out about a relationship
- Relationships can also be rules such as:
 - Two people are sisters if they are both female AND they have the same parents.
- In traditional programming relationship may be defined as
 - A and B are sisters if A and B are both female AND they have the same father AND they have the same mother AND A is not the same as B
- A rule allows us to find out about a relationship even if the relationship is not explicitly stated as a fact

Programming prolog

- Declare facts describing explicit relationships between objects and properties objects might have (e.g. Subodh likes pizza, sky has_colour blue)
- Declare rules defining implicit relationships between objects and/or rules defining implicit object properties (e.g. X is a parent if there is a Y such that Y is a child of X).
- Then the system can be used by:
 - Asking questions above relationships between objects, and/or about object properties (e.g. does Subodh like pizza? is Ayesha a parent?)

Prolog & Predicate logic

- Prolog is a programming language based on predicate logic.
 - A Prolog program attempts to prove a goal, such as brother(Barney,x), from a set of facts and rules.
 - In the process of proving the goal to be true, using substitution and the other rules
 of inference, Prolog substitutes values for the variables in the goal, thereby "computing" an answer.
- How does Prolog know which facts and which rules to use in the proof?
 - Prolog uses unification to determine when two clauses can be made equivalent by a substitution of variables.
 - The unification procedure is used to instantiate the variables in a goal clause based on the facts and rules in the database.

Tools

- **GNU prolog -** gplc, gprolog
- SWI-Prolog https://swi-prolog.org
- Online tool
 - https://swish.swi-prolog.org/
 - https://www.onlinegdb.com/online_prolog_compiler

A simple Prolog program

```
male(albert).
male(edward).
female(alice).
female(victoria).
parent(albert,edward).
parent(victoria,edward).
father(X,Y):- parent(X,Y), male(X).
\% \forall X \forall Y ((parent(X,Y) \land male(X)) \rightarrow father(X,Y))
mother(X,Y):- parent(X,Y), female(X).
\% \forall X \forall Y ((parent(X,Y) \land female(X)) \rightarrow mother(X,Y))
```

- A fact/rule (statement) ends with "." and white space ignored
- Read ':-' after RULE HEAD as "if"
- Read comma in body as "and"
- Comment a line with % or use /* */ for multi-line comments

Facts & Rules

- The Prolog environment maintains a set of facts and rules in its database.
 - Facts are axioms; relations between terms that are assumed to be true.
 - Rules are theorems that allow new inferences to be made.

Facts & Rules

- The Prolog environment maintains a set of facts and rules in its database.
 - Facts are axioms; relations between terms that are assumed to be true.
 - Rules are theorems that allow new inferences to be made.
- Example facts & rules:
 - male(adam).
 - female(anne).
 - parent(adam,barney).
 - son(X,Y):-parent(Y,X), male(X).
 - daughter(X,Y) :- parent(Y,X) , female(X).
- The first rule is read as follows: for all X and Y, X is the son of Y if there exists X and Y such that Y is the parent of X and X is male. ∀X∀Y((parent(Y, X) ∧ male(X)) → son(X, Y))
- The second rule is read as follows: for all X and Y, X is the daughter of Y if there exists X and Y such that Y is the parent of X and X is female. ∀X∀Y((parent(Y, X) ∧ female(X)) → daughter(X, Y))

Horn clauses

- To simplify the resolution process in Prolog, statements must be expressed in a simplified form, called Horn clauses.
 - Statements are constructed from terms.
 - Each statement (clause) has (at most) one term on the left hand side of an implication symbol (:-).
 - Each statement has a conjunction of zero or more terms on the right hand side.
 - Example: $p_1 \wedge p_2 \wedge \ldots \rightarrow q \equiv \neg p_1 \vee \neg p_2 \vee \ldots \vee q$
- Prolog has three kinds of statements, corresponding to the structure of the Horn clause used.
 - A fact is a clause with an empty right hand side.
 - A question (or goal) is a clause with an empty left hand side.
 - A rule is a clause with terms on both sides.

Execution of Prolog program

```
male(albert).
male(edward).
female(alice).
female(victoria).
parent(albert,edward).
parent(victoria,edward).
father(X,Y):-parent(X,Y), male(X).
mother(X,Y):-parent(X,Y), female(X).
```

```
$> gplc family.pl
$> ./family
?- male(albert).
yes
?- male(victoria).
no
?- male(subodh).
no
?- male(X).
X = albert ? :
X = edward
?- father(F,C).
F=albert, C=edward ? ;
no
```

Observation about Prolog rules

- The implication is from right to left
- The scope of a variable is the clause in which it appears.
- Variables whose first appearance is on the left hand side of the clause have implicit universal quantifiers.
- Variables whose first appearance is on the right hand side of the clause have implicit existential quantifiers.

Basic syntax of Prolog: Terms

- Constants:
 - Identifiers sequences of letters, digits, or "_" that start with lower case letters.
 - Numbers 1.001
 - Strings enclosed in single quotes
 - Can start with upper case letter or can be a number now treated as a string
- Variables:
 - Sequence of letters digits or "_" that start with an upper case letter or the _
 - Underscore by itself is the special "anonymous" variable
- Structures (like function applications)
 - <identifier>(Term-1,...,Term-k)
 - date(20,April,2020), point(X,Y,Z)
 - Definition can be recursive, so each term can itself be a structure
 - date(+(5,15),April,+(2000,-(140,120)))
 - Structures can be represented as tree

Arithmetic and logical operators

- Arithmetic operations: +, -, *, /
 - The "is" operator forces arithmetic evaluation
 - ?-X is 3+8.
- Logical operators: >, <, >=, <=
 - x =:= y (equality check)
 - x =\= y (inequality check)

Syntax of Prolog: Lists

- Lists are a very useful data structure in Prolog
- Lists are structured terms represented in a special way [a, b, c, d]
 - This is actually structured term [a | [b | [c | [d | []]]]]
 - In the above [] denotes empty list
 - Each list is thus of the form [<head> | <tail>]
 - <head> is an element of the list (not necessary a list itself)
 - <tail> is a list / sublist
 - Also, [a,b,c,d] = [a | [b,c,d]] = [a,b | [c,d]] = [a,b,c | [d]]
- This structure has important implications when it comes to matching variables against lists!

Syntax of Prolog: Predicates

- Predicates are syntactically identical to structured items <identifier>(Term-1,...,Term-k)
 - male(edward)
 - parent(edward,albert)
 - taller_than(subodh,shyam)
 - likes(X)
 - Note that X is a variable. X can take on any term as value so that this fact asserts
- Facts make assertion

Syntax of Prolog: Facts and Rules

- Rules: PredicateH:- predicate-1, ..., predicate-k.
 - First predicate is rule head. Terminated by a period
 - Rules encode ways of deriving or computing a new fact
 - animal(X):- elephant(X). X can be concluded to be animal if it shown that X is elephant
 - taller_than(X,Y) :- height(X,H1), height(Y,H2), H1 > H2.
 - father(X,Y) :- parent(X,Y), male(X).

Operation of Prolog

- A query is a sequence of predicates: predicate-1, predicate-2, ..., predicate-k
- Prolog tries to prove that this sequence of predicates is true using the facts and rules in the Prolog Program.
- In proving the sequence it performs the computation you want.
- Example:
 - elephant(fred).
 - elephant(mary).
 - elephant(joe).
 - animal(fred) :- elephant(fred).
 - animal(mary) :- elephant(mary).
 - animal(joe) :- elephant(joe).
 - QUERY: animal(fred), animal(mary), animal(joe).

Operation

- Starting with the first predicate P1 of the query Prolog examines the program from TOP to BOTTOM.
- It finds the first RULE HEAD or FACT that matches P1
- Then it replaces P1 with the RULE BODY.
- If P1 is matched a FACT, we can think of FACTs as having empty bodies (so P1 is simply removed).
- The result is a new query.
- Example
 - P1:- Q1, Q2, Q3.
 - QUERY: P1, P2, P3.
 - P1 matches with the rule, therefore, new QUERY: Q1, Q2, Q3, P2, P3.

Execution of Prolog program

```
elephant(fred).
elephant(mary).
elephant(joe).
animal(fred):- elephant(fred).
animal(mary):- elephant(mary).
animal(joe):- elephant(joe).
QUERY: animal(fred), animal(mary), animal(joe).
```

```
    elephant(fred), animal(mary), animal(joe).
    animal(mary), animal(joe).
    elephant(mary), animal(joe).
    animal(joe).
    elephant(joe).
```

EMPTY QUERY

Operation

- If this process reduces the query to the empty query, Prolog returns "yes".
- However, during this process each predicate in the query might match more than one fact or rule head
 - Prolog always choose the first match it finds. Then if the resulting query reduction did not succeed (i.e., we hit a predicate in the query that does not match any rule head of fact), Prolog backtracks and tries a new match.

Execution of Prolog program

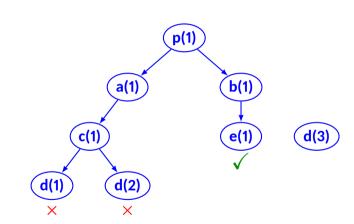
```
ant_eater(fred).
animal(fred) :- elephant(fred).
animal(fred) :- ant_eater(fred).
QUERY: animal(fred)
```

```
    elephant(fred).
    FAIL BACKTRACK
    ant_eater(fred).
    EMPTY QUERY
```

Operation

• Backtracking can occur at every stage as the query is processed

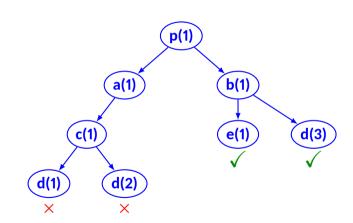
```
p(1) := a(1).
p(1) := b(1).
a(1) := c(1).
c(1) := d(1).
c(1) := d(2).
b(1):-e(1).
e(1).
d(3).
QUERY: p(1)
```



Operation

• With backtracking we can get more answers by using ";"

```
p(1) := a(1).
p(1) := b(1).
a(1) := c(1).
c(1) := d(1).
c(1) := d(2).
b(1):-e(1).
b(1) := d(3).
e(1).
d(3).
QUERY: p(1)
```



Variables and Matching

- Variables allow us to
 - Compute more than yes/no answer, compress the program
- Example:
 - elephant(fred).
 - elephant(mary).
 - elephant(joe).
 - animal(fred) :- elephant(fred).
 - animal(mary) :- elephant(mary).
 - animal(joe) :- elephant(joe).
- The three rules can be replaced by the single rule animal(X):- elephant(X).
- When matching queries against rule heads (of facts) variables allow many additional matches.

Example

```
elephant(fred).
elephant(mary).
elephant(joe).
animal(X):- elephant(X).
QUERY: animal(fred), animal(mary), animal(joe)
```

- 1. X=fred, elephant(X), animal(mary), animal(joe)
- 2. animal(mary), animal(joe)
- 3. X=mary, elephant(X), animal(joe)
- 4. animal(joe)
- 5. X=joe, elephant(X)
- 6. EMPTY QUERY

Operation with Variables

- Queries are processed as before (via rule and fact matching and backtracking), but now we can use variables to help us match rule heads or facts.
- A query predicate matches a rule head or fact (either one with variables) if
 - The predicate name must match. So elephant(X) can match elephant(joe), but can never match ant_eater(joe).
 - Then, the arity of the predicates are matched (number of terms). So foo(X,Y) can match foo(joe,mary), but cannot match foo(joe) or foo(joe,mary,fred).
 - If the predicate names and arities match then each of the k-terms match. So for foo(t1, t2, t3) to match foo(s1, s2, s3) we must have that t1 matches s1, t2 matches s2, and t3 matches t3.
 - During this matching process we might have to "bind" some of the variables to make the terms match.
 - These bindings are then passed on into the new query (consisting of the rule body and the left over query predicates).

Variable matching (Unification)

- Two terms with variables match if :
 - If both are constants (identifiers, numbers, or strings) and are identical
 - If one or both are bound variables then they match if what the variables are bound to match
 - X and mary where X is bound to the value mary will match
 - X and Y where X is bound to mary and Y is bound to mary will match
 - X and ann where X is bound to mary will not match
 - If one of the terms is an unbound variable then they match and we bind the variable to the term
 - X and mary where X is unbound match and make X bound to mary.
 - X and Y where X is unbound and Y is bound to mary match and make X bound to mary.
 - X and Y where both X and Y are unbound match and make X bound to Y (or vice versa).

Solving queries

- Prolog work as follows
 - Unification
 - Goal directed reasoning
 - Rule ordering
 - DFS and backtracking

- Much of prolog's computation is organized around lists. Two key things we do with a list is iterate over them and build new ones.
- Checking membership: member(X,Y) X is a member of list Y

- Much of prolog's computation is organized around lists. Two key things we do with a list is iterate over them and build new ones.
- Checking membership: member(X,Y) X is a member of list Y
 - member(X,[X|_]).
 - member(X,[_|T]) :- member(X,T).

- Much of prolog's computation is organized around lists. Two key things we do with a list is iterate over them and build new ones.
- Checking membership: member(X,Y) X is a member of list Y
 - member(X,[X|_]).
 - member(X,[_|T]) :- member(X,T).
- Building a list of integers in range [i,j] (build(from, to, NewList))

- Much of prolog's computation is organized around lists. Two key things we do with a list is iterate over them and build new ones.
- Checking membership: member(X,Y) X is a member of list Y
 - member(X,[X|_]).
 - member(X,[_|T]) :- member(X,T).
- Building a list of integers in range [i,j] (build(from, to, NewList))
 - build(I,J,[]) :- I>J.
 - build(I,J,[I | Rest]) :- I =< J, N is I+1, build(N,J,Rest).

List examples

• Concatenation: concatenation(X, Y, Z)

List examples

- Concatenation: concatenation(X, Y, Z)
 - concatenation([], L, L).
 - concatenation([X|L1], L2, [X|L3]) :- concatenation(L1, L2, L3).

List examples

- Concatenation: concatenation(X, Y, Z)
 - concatenation([], L, L).
 - concatenation([X|L1], L2, [X|L3]) :- concatenation(L1, L2, L3).
- Example:
 - concatenation([a,b], [c,d], Y).

- Concatenation: concatenation(X, Y, Z)
 - concatenation([], L, L).
 - concatenation([X|L1], L2, [X|L3]) :- concatenation(L1, L2, L3).
- Example:
 - concatenation([a,b], [c,d], Y).
 - X=a, concatenation([X|b], [c,d], [X|Y1]).
 - concatenation([b], [c,d], Y1).
 - X=b, concatenation([X|[]], [c,d], [X|Y2]).
 - concatenation([], [c,d], Y2).

- Adding in front: add(X, Y, Z) add X in front of Y and result into Z
 - add(X, L, [X|L]).

- Adding in front: add(X, Y, Z) add X in front of Y and result into Z
 - add(X, L, [X|L]).
- Deletion: del(X, Y, Z) delete X from Y and store result in Z

- Adding in front: add(X, Y, Z) add X in front of Y and result into Z
 - add(X, L, [X|L]).
- Deletion: del(X, Y, Z) delete X from Y and store result in Z
 - del(X, [X | Tail], Tail).
 - del(X, [Y|Tail], [Y|Tail1]) :- del(X, Tail, Tail1).

- Adding in front: add(X, Y, Z) add X in front of Y and result into Z
 - add(X, L, [X|L]).
- Deletion: del(X, Y, Z) delete X from Y and store result in Z
 - del(X, [X | Tail], Tail).
 - del(X, [Y|Tail], [Y|Tail1]) :- del(X, Tail, Tail1).
- Sublist: sublist(S, L) check whether S is sublist of L

- Adding in front: add(X, Y, Z) add X in front of Y and result into Z
 - add(X, L, [X|L]).
- Deletion: del(X, Y, Z) delete X from Y and store result in Z
 - del(X, [X|Tail], Tail).
 - del(X, [Y|Tail], [Y|Tail1]) :- del(X, Tail, Tail1).
- Sublist: sublist(S, L) check whether S is sublist of L
 - sublist(S, L):- concatenation(L1, L2, L), concatenation(S, L3, L2).

- Adding in front: add(X, Y, Z) add X in front of Y and result into Z
 - add(X, L, [X|L]).
- Deletion: del(X, Y, Z) delete X from Y and store result in Z
 - del(X, [X|Tail], Tail).
 - del(X, [Y|Tail], [Y|Tail1]) :- del(X, Tail, Tail1).
- Sublist: sublist(S, L) check whether S is sublist of L
 - sublist(S, L):-concatenation(L1, L2, L), concatenation(S, L3, L2).
- GCD: gcd(X, Y, Z)
 - gcd(X,X,X).
 - gcd(X,Y,Z) :- X < Y, Y1 is Y-X, gcd(X,Y1,Z).

- Permutation:
 - permutation([], []).
 - permutation([X|L], P):-permutation(L, L1), insert(X, L1, P).

- Solution:
 - solution(Queens):- permutation([1,2,3,4,5,6,7,8], Queens), safe(Queens).

- Solution:
 - solution(Queens):- permutation([1,2,3,4,5,6,7,8], Queens), safe(Queens).
- Permutation:
 - permutation([],[]).
 - permutation([Head | Tail], PermList) :permutation(Tail, Permtail), del(Head, PermList, Permtail).

- Solution:
 - solution(Queens):- permutation([1,2,3,4,5,6,7,8], Queens), safe(Queens).
- Permutation:
 - permutation([],[]).
 - permutation([Head | Tail], PermList) :permutation(Tail, Permtail), del(Head, PermList, Permtail).
- Safe:
 - safe([]).
 - safe([Queen|Others]):- safe(Others), noattack(Queen, Others, 1).

- Solution:
 - solution(Queens):- permutation([1,2,3,4,5,6,7,8], Queens), safe(Queens).
- Permutation:
 - permutation([],[]).
 - permutation([Head | Tail], PermList):permutation(Tail, Permtail), del(Head, PermList, Permtail).
- Safe:
 - safe([]).
 - safe([Queen | Others]) :- safe(Others), noattack(Queen, Others, 1).
- No-attack:
 - noattack(_,[],_).
 - noattack(Y,[Y1|Ylist],Xdist): Y-Y1 =\= Xdist, Y1-Y=\= Xdist, Dist is Xdist+1, noattack(Y, Ylist, Dist).

Cuts - controlled backtracking

```
C:-P, Q, R, !, S, T, U.
C:-V.
A:-B, C, D.
?-A.
```

- Backtracking within the goal list P, Q, R
- As soon as the cut is reached:
 - All alternatives of P, Q, R are suppressed
 - The clause C :- V will also be discarded
 - Backtracking is possible within S, T, U.
 - No effect for rule A, that is backtracking within B, C, D remains active.

Cuts

- del_duplicates([], []).
- del_duplicates([Head | Tail], Result) :member(Head, Tail), !, del_duplicates(Tail, Result). % R1
- del_duplicates([Head | Tail], [Head | Result]) :- del_duplicates(Tail, Result). % R2

Cuts - Example

- If X >= Y then Max=X, otherwise Max=Y
 - max(X, Y, X) :- X>=Y, !.
 - max(X, Y, Y).
- Adding an element into a list without duplication
 - add(X, L, L) :- member(X,L), !.
 - add(X, L, [X|L]).

Thank you!