### **Introduction to Deep Learning**



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#### **Convolutional Neural Network**

#### Introduction

- Specialized neural network for processing data that has grid like topology
  - Time series data (one dimensional)
  - Image (two dimensional)
- Found to be reasonably suitable for certain class of problems eg. computer vision
- Instead of matrix multiplication, it uses convolution in at least one of the layers

### Convolution operation

- Consider the scenario of locating a spaceship with a laser sensor
- Suppose, the sensor is noisy
  - Accurate estimation is not possible
- Weighted average of location can provide a good estimate s(t) $\int x(a)w(t-a)da$ 
  - x(a) Location at age a by the sensor, t current time, w weight
  - This is known as convolution
  - Usually denoted as s(t) = (x \* w)(t)
- In neural network terminology x is input, w is kernel and output is referred as feature map

### **Convolution operation (contd)**

• Discrete convolution can be represented as

$$s(t) = (x * w)(t) = \sum x(a)w(t-a)$$

- In neural network input is multidimensional and so is kernel
  - These will be referred as tensor
- Two dimensional convolution can be defined as

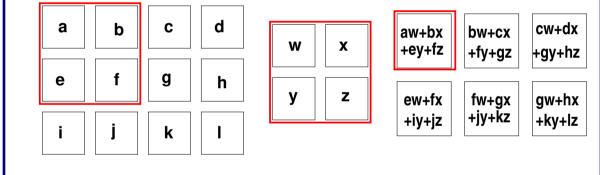
$$s(i,j) = (I * K)(i,j) = \sum I(m,n)k(i-m,j-n) = \sum I(i-m,j-n)k(m,n)$$

- Commutative
- In many neural network, it implements as cross-correlation

$$s(i,j) = (I * K)(i,j) = \sum \sum I(i+m,j+n)k(m,n)$$

No kernel flip is possible

### 2D convolution

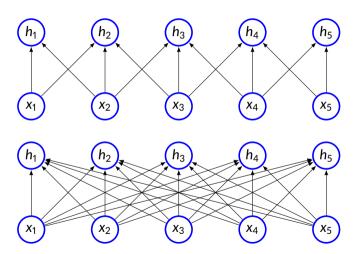


#### **Advantages**

- Convolution can exploit the following properties
  - Sparse interaction (Also known as sparse connectivity or sparse weights)
  - Parameter sharing
  - Equivariant representation

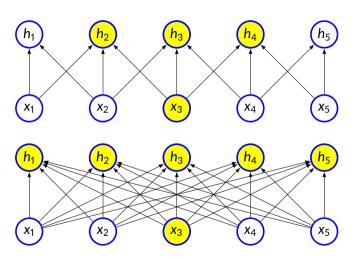
### Sparse interaction

- Traditional neural network layers use matrix multiplication to describe how outputs and inputs are related
- Convolution uses a smaller kernel
  - Significant reduction in number of parameters
  - Computing output require few comparison
- For example, if there is m inputs and n outputs, traditional neural network will require  $m \times n$  parameters
- If each of the output is connected to at most k units, the number of parameters will be  $k \times n$



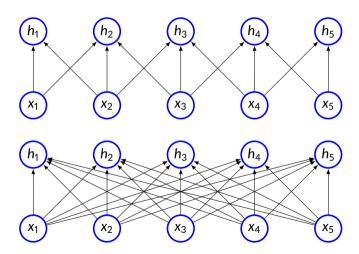
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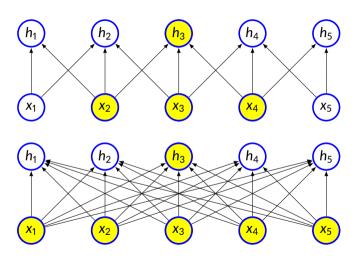
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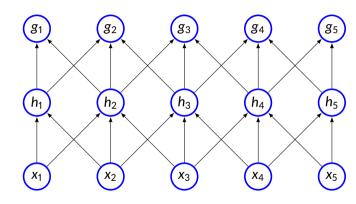
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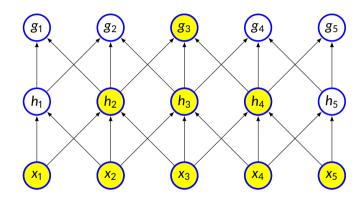




# Receptive field



# Receptive field

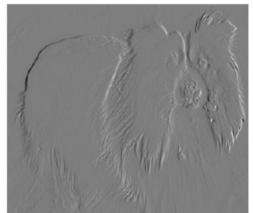


#### Parameter sharing

- Same parameters are used for more than one function model
- In tradition neural network, weight is used only once
- Each member of kernel is used at every position of the inputs
- As  $k \ll m$ , the number of parameters will reduced significantly
- Also, require less memory

# **Edge detection**





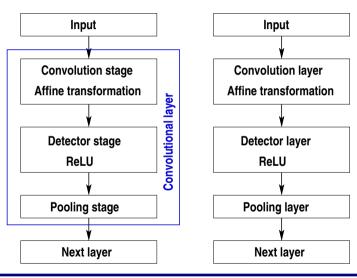
#### **Equivariance**

- If the input changes, the output changes in the same
- Specifically, a function f(x) is equivariant to function g if f(g(x)) = g(f(x))
  - Example, g is a linear translation
  - Let B be a function giving image brightness at some integer coordinates and g be a function mapping from one image to another image function such that l' = g(l) with l'(x, y) = l(x 1, y)
- There are cases sharing of parameters across the entire image is not a good idea

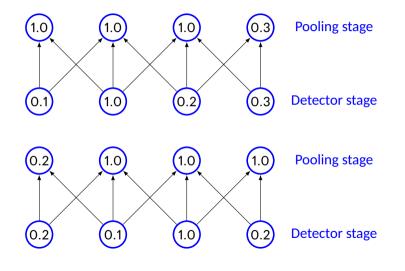
### Pooling

- Typical convolutional network has three stages
  - Convolution several convolution to produce linear activation
  - Detector stage linear activation runs through the non-linear unit such as ReLU
  - Pooling Output is updated with a summary of statistics of nearby inputs
    - Maxpooling reports the maximum output within a rectangular neighbourhood
    - Average of rectangular neighbourhood
    - Weighted average using central pixel
- Pooling helps to make representation invariant to small translation
  - Feature is more important than where it is present
- Pooling helps in case of variable size of inputs

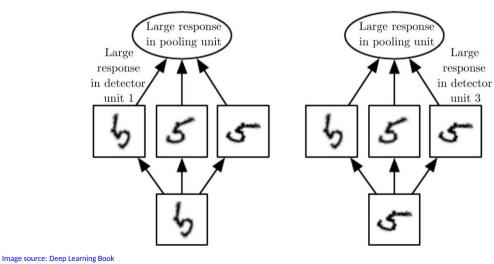
### Typical CNN



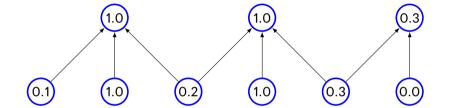
# Invariance of maxpooling



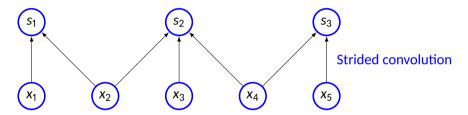
#### Learned invariances



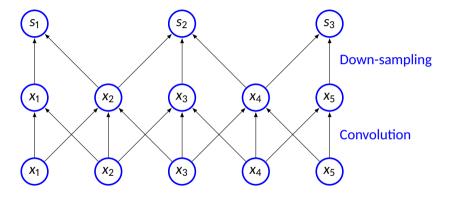
# Pooling with downsampling



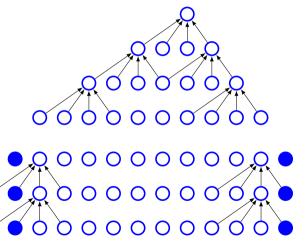
### Strided convolution



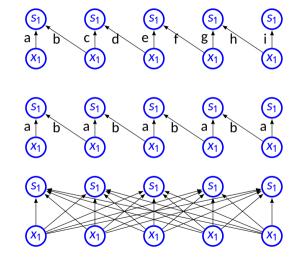
# Strided convolution (contd)



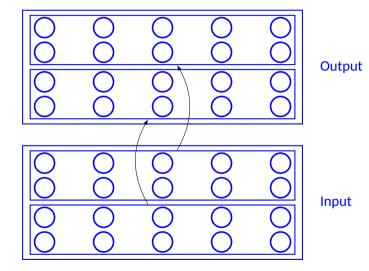
# Zero padding



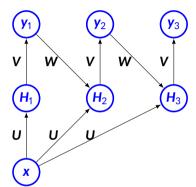
### Connections



# **Local convolution**



### Recurrent convolution network



### **AlexNet**

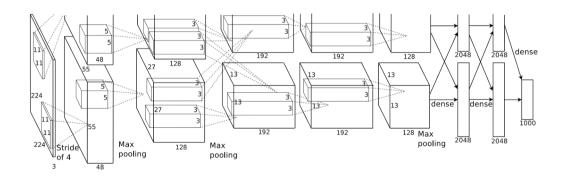


Image source: https://worksheets.codalab.org

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## GoogleNet

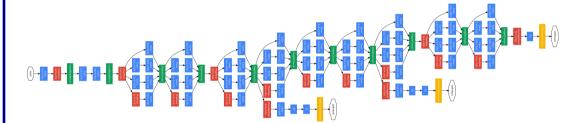
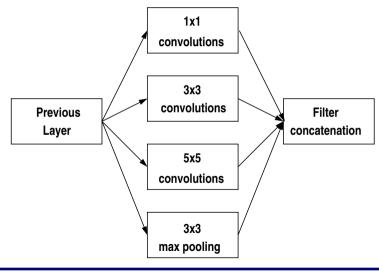


Image source: http://joelouismarino.github.io

### Naive inception



### Inception

