# **Introduction to Deep Learning**



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### **Convolutional Neural Network**

#### Introduction

- Specialized neural network for processing data that has grid like topology
  - Time series data (one dimensional)
  - Image (two dimensional)
- Found to be reasonably suitable for certain class of problems eg. computer vision
- Instead of matrix multiplication, it uses convolution in at least one of the layers

- Consider the scenario of locating a spaceship with a laser sensor
- Suppose, the sensor is noisy
  - Accurate estimation is not possible
- Weighted average of location can provide a good estimate  $s(t) = \int x(a)w(t-a)da$ 
  - x(a) Location at age a by the sensor, t current time, w weight
  - This is known as convolution
  - Usually denoted as s(t) = (x \* w)(t)
- In neural network terminology x is input, w is kernel and output is referred as feature map

### **Convolution operation (contd)**

Discrete convolution can be represented as

$$s(t) = (x * w)(t) = \sum_{a=\infty}^{\infty} x(a)w(t-a)$$

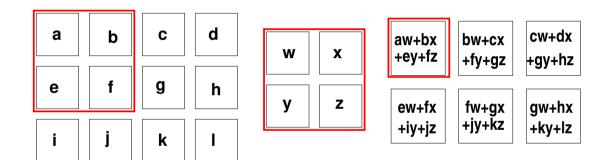
- In neural network input is multidimensional and so is kernel
  - These will be referred as tensor
- Two dimensional convolution can be defined as

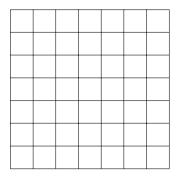
$$s(i,j) = (I * K)(i,j) = \sum_{m,n} I(m,n)k(i-m,j-n) = \sum_{m,n} I(i-m,j-n)k(m,n)$$

- Commutative
- In many neural network, it implements as cross-correlation

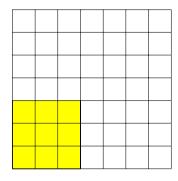
$$s(i,j) = (I*K)(i,j) = \sum \sum I(i+m,j+n)k(m,n)$$

• No kernel flip is possible





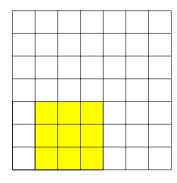
Grid size:  $7 \times 7$ 



Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

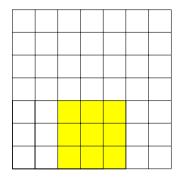
Stride: 1



Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

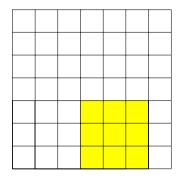
Stride: 1



Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

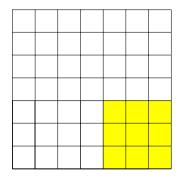
Stride: 1



Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

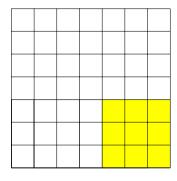
Stride: 1



Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

Stride: 1

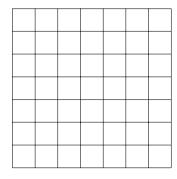


Grid size:  $7 \times 7$ 

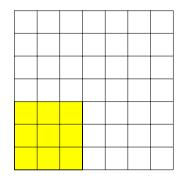
Filter size:  $3 \times 3$ 

Stride: 1

Output size:  $5 \times 5$ 



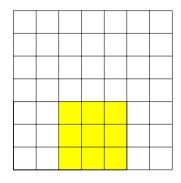
Grid size:  $7 \times 7$ 



Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

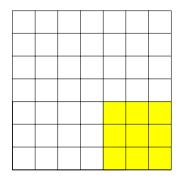
Stride: 2



Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

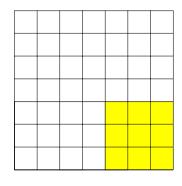
Stride: 2



Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

Stride: 2

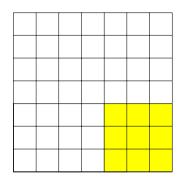


Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

Stride: 2

Output size:  $3 \times 3$ 



Grid size:  $7 \times 7$ 

Filter size:  $3 \times 3$ 

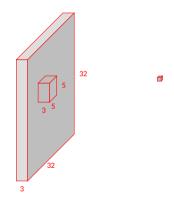
Stride: 2

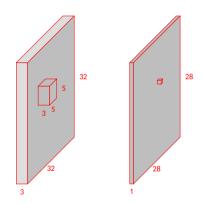
Output size:  $3 \times 3$ 

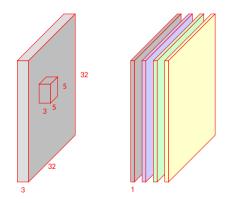
Output size: (N - F)/S + 1

N - input size, F - Filter size,

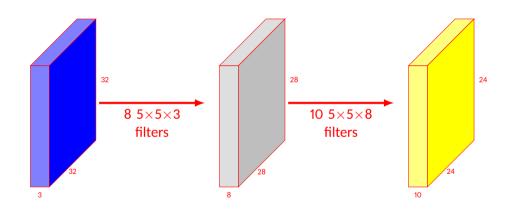
S - Stride





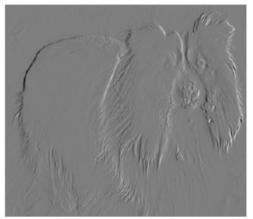


### **Convolution example**



# **Edge detection**



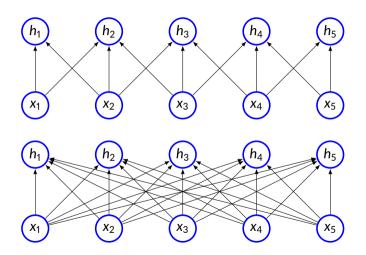


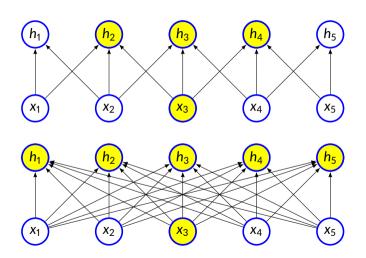
### **Advantages**

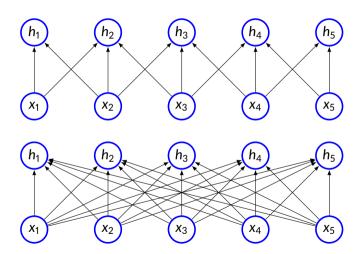
- Convolution can exploit the following properties
  - Sparse interaction (Also known as sparse connectivity or sparse weights)
  - Parameter sharing
  - Equivariant representation

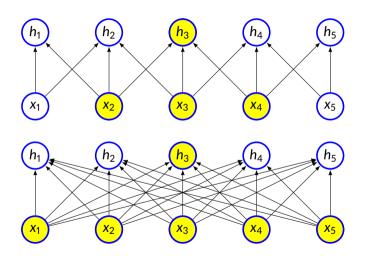
### **Sparse interaction**

- Traditional neural network layers use matrix multiplication to describe how outputs and inputs are related
- Convolution uses a smaller kernel
  - Significant reduction in number of parameters
  - Computing output require few comparison
- For example, if there is m inputs and n outputs, traditional neural network will require  $m \times n$  parameters
- If each of the output is connected to at most k units, the number of parameters will be  $k \times n$

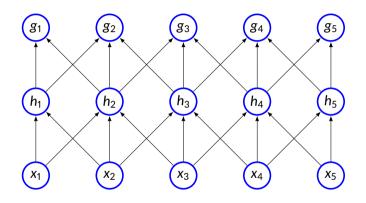




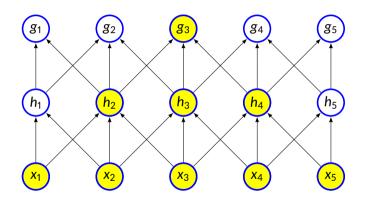




# **Receptive field**



# **Receptive field**



#### **Parameter sharing**

- Same parameters are used for more than one function model
- In tradition neural network, weight is used only once
- Each member of kernel is used at every position of the inputs
- As  $k \ll m$ , the number of parameters will reduced significantly

Also, require less memory

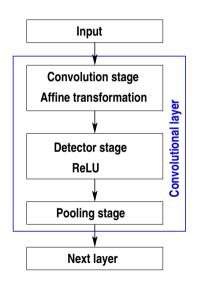
#### **Equivariance**

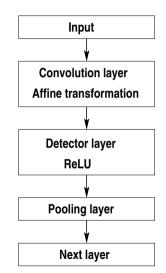
- If the input changes, the output changes in the same way
- Specifically, a function f(x) is equivariant to function g if f(g(x)) = g(f(x))
  - Example, g is a linear translation
  - Let B be a function giving image brightness at some integer coordinates and g be a function mapping from one image to another image function such that l' = g(l) with l'(x, y) = l(x 1, y)
- There are cases sharing of parameters across the entire image is not a good idea

### **Pooling**

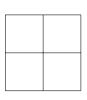
- Typical convolutional network has three stages
  - Convolution several convolution to produce linear activation
  - Detector stage linear activation runs through the non-linear unit such as ReLU
  - Pooling Output is updated with a summary of statistics of nearby inputs
    - Maxpooling reports the maximum output within a rectangular neighbourhood
    - Average of rectangular neighbourhood
    - Weighted average using central pixel
- Pooling helps to make representation invariant to small translation
  - Feature is more important than where it is present
- Pooling helps in case of variable size of inputs

### **Typical CNN**

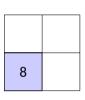




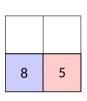
0	4	7	8
9	2	4	5
6	7	3	4
8	2	1	5



О	4	7	8
9	2	4	5
6	7	3	4
8	2	1	5



О	4	7	8
9	2	4	5
6	7	3	4
8	2	1	5



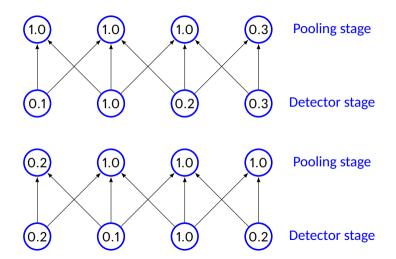
0	4	7	8
9	2	4	5
6	7	3	4
8	2	1	5



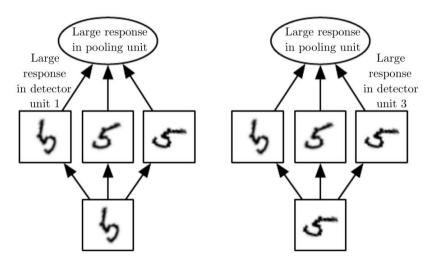
0	4	7	8
9	2	4	5
6	7	3	4
8	2	1	5

9	8
8	5

## **Invariance of maxpooling**



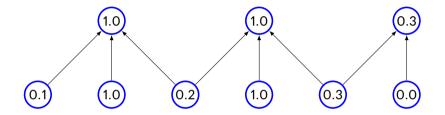
#### **Learned invariances**



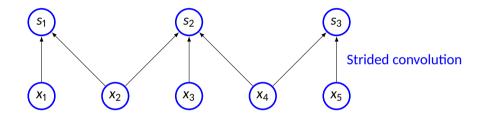
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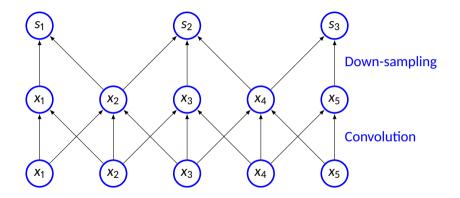
## **Pooling with downsampling**



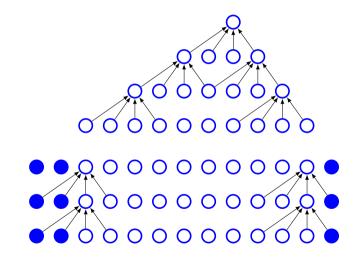
## **Strided convolution**



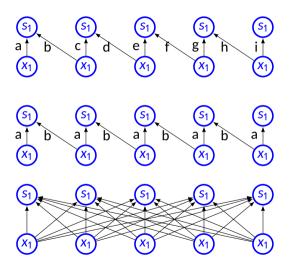
## **Strided convolution (contd)**



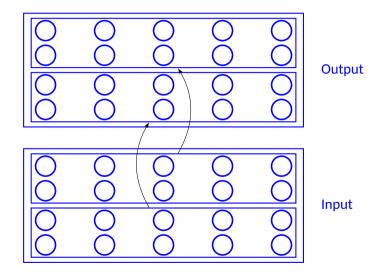
## Zero padding



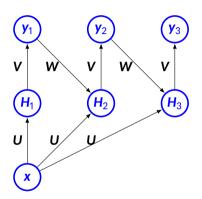
### **Connections**



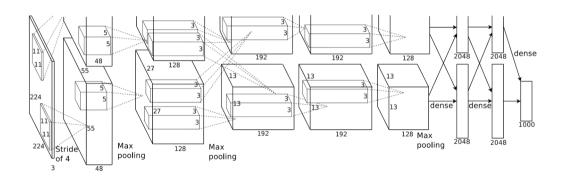
## **Local convolution**



#### **Recurrent convolution network**



### **AlexNet**



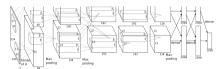
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#### **AlexNet**

#### Architecture

- INPUT  $227 \times 227 \times 3$
- CONV1 96 11 × 11 filters at stride 4, pad 0. Output: 55 × 55 × 96
- MAX POOL1 3 × 3 filter, stride 2 Output: 27 × 27 × 96
- **NORM1 Output:** 27 × 27 × 96
- CONV2 256 5 × 5 filters at stride 1, pad
  2, Output: 27 × 27 × 256
- MAX POOL2  $3 \times 3$  filter, stride 2 Output:  $13 \times 13 \times 256$
- NORM2  $0.13 \times 13 \times 256$



- CONV3 384 3 × 3 filter, stride 1, pad 1,
  Output: 13 × 13 × 384
- CONV4 384  $3 \times 3$  filter, stride 1, pad 1, Output:  $13 \times 13 \times 384$
- CONV5 256  $3 \times 3$  filter, stride 1, pad 1, Output:  $O 13 \times 13 \times 256$
- MAX POOL3 3 × 3 filter, stride 2, Output: 6 × 6 × 256
- FC6 4096 Neurons
- FC7 4096 Neurons
- FC8 1000 Neurons

# VggNet

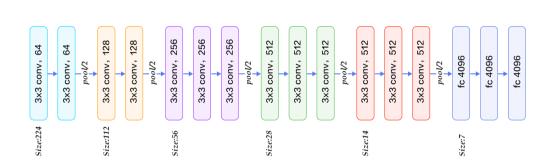
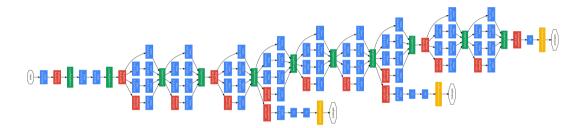


Image source: internet

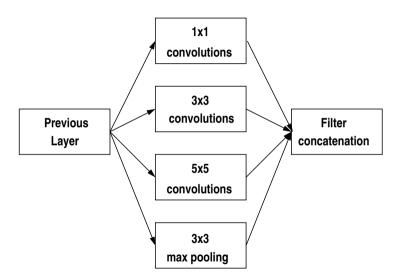
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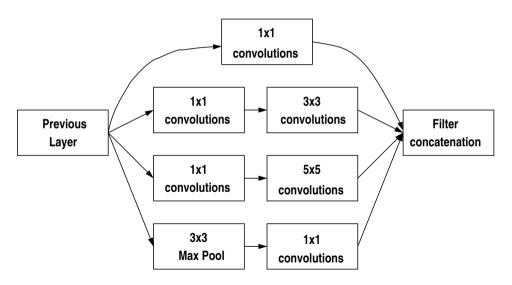
## **GoogleNet**



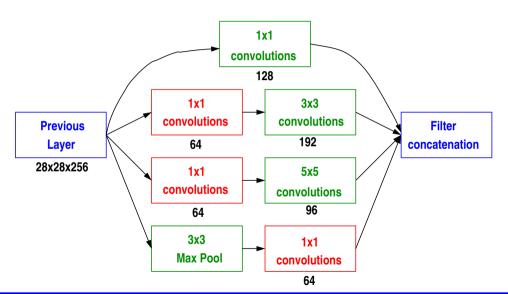
## **Naive inception**



## **Inception**



## Inception



#### **ResNet**

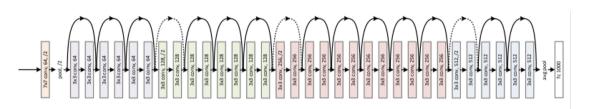
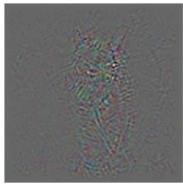


Image source: internet

## **Comparison of CNN architecture**

Model	Size (M)	Top-1/top-5 error (%)	# layers	Model description
AlexNet	238	41.00/18.00	8	5  conv + 3  fc layers
VGG-16	540	28.07/9.33	16	13  conv + 3  fc layers
VGG-19	560	27.30/9.00	19	16  conv + 3  fc layers
GoogleNet	40	29.81/10.04	22	21  conv + 1  fc layers
ResNet-50	100	22.85/6.71	50	49 conv + 1 fc layers
ResNet-152	235	21.43/3.57	152	151 conv + 1 fc layers

# **Guided backpropagation**



Backprop



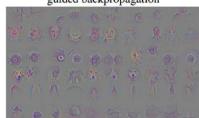
**Guided Backprop** 

## **Guided backpropagation**

guided backpropagation



guided backpropagation



corresponding image crops



corresponding image crops



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## **Fantasy image**







cup

dalmatian